THE DARK ENERGY SURVEY: PROSPECTS FOR RESOLVED STELLAR POPULATIONS


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ABSTRACT

Wide angle and deep surveys, regardless of their primary purpose, always sample a large number of stars in the Galaxy and in its satellite system. Here we make a forecast of the expected stellar sample resulting from the Dark Energy Survey (DES) and the perspectives that it will open for studies of Galactic structure and resolved stellar populations in general. An estimated $1.2 \times 10^7$ stars will be sampled in DES grizY filters in the southern equatorial hemisphere. This roughly corresponds to 20% of all DES sources. Most of these stars belong to the stellar thick disk and halo of the Galaxy. DES will probe low-mass stellar and sub-stellar objects at depths from three to eight times larger than those in the Sloan Digital Sky Survey (SDSS). The faint end of the main sequence (MS) will be densely sampled beyond 10 kpc. The slope of the low mass end of the stellar initial mass function (IMF) will be constrained to within a few hundredths of dex, even in the thick disk and halo. In the sub-stellar mass regime, the IMF slope will be potentially constrained to within $d \log \phi(m)/d \log m \simeq 0.1$. About $3 \times 10^4$ brown dwarf candidates and at least $7.6 \times 10^5$ white dwarf candidates will be selected, the latter embedded into the thick disk and halo, for future follow-up. The stellar halo flattening will also be constrained to within a few percent. DES will probe the MS of new Milky Way satellites and halo clusters for distances out to $\simeq 120$ kpc, therefore yielding stellar surface density contrasts 1.6–1.7 times larger than those attainable with SDSS. It will also allow detection of these objects in the far reaches of the stellar halo, substantially increasing the number and quality of probes to the Galactic potential. Combined with northern samples, such as the SDSS, the DES stellar sample will yield constraints on the structure and stellar populations of Galactic components in unprecedented detail. In particular, the combined sample from both hemispheres will allow detailed studies of halo and thick disk asymmetries and triaxiality.

Key words: Galaxy: stellar content – Galaxy: structure – stars: statistics

1. INTRODUCTION

Wide angle photometric surveys have been of enormous value in studies of the structure and history of the formation of our Galaxy. Surveys such as the Two Micron All-Sky Survey (2MASS; Skrutskie et al. 1997) and the Sloan Digital Sky Survey (SDSS; York et al. 2000) have brought a substantial increase in the size and depth of homogenous stellar samples. As a consequence, the structural parameters of the Galaxy have also revealed the complexity of substructure in the Galactic halo (e.g., Koposov et al. 2008; Walsh et al. 2009; Rocha-Pinto et al. 2004; Sharma et al. 2010).

A new generation of wide angle and deep surveys is underway. In the infrared, the UKIRT Infra-Red Deep Sky Survey (Lawrence et al. 2007) is covering 7500 deg$^2$ of the northern celestial hemisphere in JHK, reaching about 3 mag deeper than 2MASS. Its ability to see through the high dust extinction regions is allowing new discoveries in previously unexplored Galactic depths (e.g., Lucas & Samuel 2010). The Visible and Infrared Survey Telescope for Astronomy (VISTA) will carry out several surveys in the near-infrared ZYJHKs bands during the upcoming years. In particular, the Vista Hemisphere Survey will cover the entire southern sky in $J$ and $K_s$, and a smaller region in $H$, with limiting magnitudes reaching $J = 21.2$, $H = 20.6$, and $K_s = 20.0$. The VISTA Magellanic Clouds Survey will sample the areas in and around these two satellites at much fainter levels than 2MASS (Cioni et al. 2008).

The Dark Energy Survey (DES) is a survey planned to start in 2011 (DePoy et al. 2008; Mohr et al. 2008). DES will cover a continuous area of 5000 deg$^2$ of the southern Galactic cap, in five (grizY) filters, to limiting magnitudes much fainter than those of SDSS over a comparable area, thus probing a much larger volume. It will use a new large field of view camera, with a mosaic of 64 CCDs of considerable efficiency in the near-infrared. The combination of a large area, depth, and red
sensitivity of the survey makes it of particular interest in the search for cool stars in the Galaxy.

Also in the optical region, the SkyMapper Southern Sky Survey (Murphy et al. 2009) will cover the entire Southern Hemisphere on six filters (ugrizy) but will be shallower than DES. On the other hand, the addition of $u$-band data is particularly important to select several types of hot stars, from horizontal branch stars to white dwarfs (WDs; Sirko et al. 2004; Harris et al. 2003).

Looking a little further into the future, when fully operational, PanSTARRSS will consist of four mirrors, each 1.8 m in diameter, simultaneously observing a $\simeq 7$ deg$^2$ field of view. In a single lunar cycle, using dark time, it will be able to scan the entire northern sky about three times. Its main goal is to detect and monitor solar system objects, especially those that can be potentially hazardous. On the other hand, its extremely large and multi-epoch database of stars and galaxies will have numerous other applications.

The Large Synoptic Survey Telescope (LSST) is an 8.5 m telescope of extremely high étendue. With a 9.6 deg$^2$ field of view, it will be capable of imaging half of the sky in six optical bands (ugrizy) once every few nights. One of its basic and unique strengths will be to discover and study transient optical phenomena, produced from a variety of astrophysical sources. With its high observational rate, LSST will also be particularly suited to detecting the non-sidereal motion of extremely faint solar system objects. Finally, its massive and deep sampling of stellar and extragalactic objects will allow research on several fields of astrophysics, from stellar to cosmology (Ivezić et al. 2008).

The goal of the present paper is to investigate the possible contributions that DES will bring to the structure of our Galaxy, to constraining key parameters describing the initial mass function (IMF) and star formation history (SFH) of different Galactic components, and to the identification of rare or faint stellar and sub-stellar objects. Our starting point for this goal is a forecast of what the DES stellar sample will look like, based on the TRILEGAL Galactic model presented by Girardi et al. (2005). A preliminary forecast of DES stellar population studies was presented by Santiago & Yanny (2010). In Section 2, we describe DES in more detail. In Section 3, we briefly review the Galaxy model used in our DES simulation and the choice of parameters adopted. We also present the expected spatial and photometric distributions within the DES footprint for different stellar types and Galactic structural components. In Section 4, we deal with the critical issue of star/galaxy separation in a deep survey like DES. In Section 5, we discuss the DES characteristic sampling depths for low-mass and/or low-luminosity stars, including M stars, WDs, and brown dwarfs (BDs). We also estimate the number of candidates of these objects to be sampled with DES under different assumptions for the stellar IMF at low-mass regimes. In Section 6, we discuss the use of proper motions (PMs) in association with DES photometric data as a tool for detecting cool WDs and to separate L and T dwarfs from high-redshift QSOs. In Section 7, we review recent results obtained for the Galactic structure, with emphasis on the thick disk and halo components. We also assess the constraints that DES will provide in determining the stellar shape of the halo and the prospects for searching for thick disk and halo asymmetries with the combined DES and SDSS samples. Finally, we discuss the perspectives brought by DES to the detection of new Milky Way (MW) satellites, clusters, and substructure in general. A summary of our results is presented in Section 8.

2. THE DARK ENERGY SURVEY

During its planned five years of operation, DES will cover 5000 deg$^2$ on the sky in grizY filters, mostly in directions with Galactic latitudes $|b| > 30\degree$. A new large field camera, DECam, is currently under construction and will be installed in the primary focus of the 4 m Blanco telescope, at Cerro Tololo Inter-American Observatory (CTIO) in order to carry out the survey. DECam is made up of 62 2k $\times$ 4k red-sensitive CCDs recently developed at Lawrence Berkeley National Laboratory. This large CCD mosaic will cover a field of view of 2.2 deg$^2$, yielding a pixel scale of 0.27 arcsec pixel$^{-1}$. Given the typical seeing at CTIO, ranging from 0.6 to 1.1 arcsec, this image scale will allow an efficient sampling of the point-spread function and its variations across the image. The expected photometric calibration accuracy is 2% over the entire survey area.

DES’s primary purpose is to constrain the cosmological parameters, most especially the matter density parameter, $\Omega_m$, and the slope of the cosmic equation of state, $w$. As such, it was designed to include the sky region to be covered by the South Pole Telescope (SPT; Carlstrom et al. 2009), in order to optically probe a potentially unbiased sample of massive galaxy clusters to high redshifts, pre-selected with the Sunyaev–Zeldovich effect (Staniszewski et al. 2009). In order to be placed in a similar photometric system as SDSS, DES will also cover SDSS’s Stripe 82 plus a connecting region between this and the SPT.

Despite its cosmological motivations, about 20% of the detected DES sources will be stars, in a total of $\simeq 10^8$, the majority of them located in the thick disk and halo of the MW. The survey’s aimed detection limits are $g = 24.6$, $r = 24.1$, $i = 24.4$, $z = 23.8$, and $Y = 21.3$ at a signal-to-noise ratio (S/N) = 10. These deep limits will allow a wide range of studies on the structure of the Galaxy and its satellite system. A first step toward assessing these contributions in detail requires a full model of the DES stellar sample. We do that in the next section.

As mentioned in Section 1, DES will be complemented in several ways by other surveys in the southern skies and on similar timescales. Most specially, it will provide $Y$-band data to the VISTA collaboration in exchange for $JHK$ data within the DES area. At shorter wavelengths, SkyMapper will cover the $u$ band, although at a shallower depth and coarser image scale. Finally, as mentioned earlier, combination of microwave SPT data and optical DES data will be very useful for galaxy clusters detection and analysis.

3. GALACTIC MODEL

In this paper, we adopt TRILEGAL to describe the structure of the Galaxy. This model provides a synthetic stellar sample for any direction of the Galaxy, including contributions from its four basic structural components: the thin and thick disks, the bulge, and the stellar halo. The code uses the Girardi et al. (2002) database of stellar isochrones, complemented with additional models for BDs (Allard et al. 2000; Chabrier et al. 2000) and WDs (Benvenuto & Althaus 1999; Finley et al. 1997; Hameier et al. 1998). More details about this Galactic model are provided in Girardi et al. (2005).

The parameters describing the various Galactic components were originally determined by comparing model predictions to a large variety of pencil beam observations (e.g., DMS, EIS-deep), shallow wide-area surveys (e.g., 2MASS), and the local sample from the Hipparcos catalog. The model calibration has
Table 1
TRILEGAL Parameters Used in This Work

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exponential thin disk</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \Sigma_{\text{thin}} )</td>
<td>59 ( M_\odot \text{pc}^{-2} )</td>
<td>Local mass surface density</td>
</tr>
<tr>
<td>( h_R )</td>
<td>2800 pc</td>
<td>Thin disk scale length</td>
</tr>
<tr>
<td>( h_z )</td>
<td>95 pc</td>
<td>Young thin disk ( \text{sech}^2 ) scale height</td>
</tr>
<tr>
<td>( h_{\text{dust}} )</td>
<td>100 pc</td>
<td>Dust scale height</td>
</tr>
<tr>
<td>Exponential thick disk</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \rho_{\text{thick}} )</td>
<td>0.004 ( M_\odot \text{pc}^{-3} )</td>
<td>Local mass density</td>
</tr>
<tr>
<td>( h_R )</td>
<td>2800 pc</td>
<td>Thick disk scale length</td>
</tr>
<tr>
<td>( h_z )</td>
<td>800 pc</td>
<td>Thick disk exponential scale height</td>
</tr>
<tr>
<td>Oblate halo</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \rho_{\text{halo}} )</td>
<td>1.5 ( \times 10^{-4} M_\odot \text{pc}^{-3} )</td>
<td>Local mass density</td>
</tr>
<tr>
<td>( r_e )</td>
<td>2800 pc</td>
<td>de Vaucouleurs radius</td>
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<tr>
<td>( c/a )</td>
<td>0.65</td>
<td>Axial ratio</td>
</tr>
<tr>
<td>Triaxial bulge</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \rho_{\text{bulge}} )</td>
<td>406 ( M_\odot \text{pc}^{-3} )</td>
<td>Central mass density</td>
</tr>
<tr>
<td>( r_e )</td>
<td>2500 pc</td>
<td>Exponential scale radius</td>
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<tr>
<td>( \theta_b )</td>
<td>15(^\circ)</td>
<td>Long axis orientation</td>
</tr>
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</table>

been extended to the bulge of our Galaxy by Vanhollebeke et al. (2009).

The basic structural parameters used to model the DES data are listed in Table 1. The fiducial model parameters for the disks, bulge, and the halo were taken from the aforementioned studies used to validate TRILEGAL itself.

The model also assumes that the Sun is at \( R_\odot = 8500 \) pc from the Galactic center and displaced by \( z_\odot = 24 \) pc from the disk mid-plane. Stars are randomly drawn from a piecewise power-law IMF as quoted by Kroupa (2001). In order to mimic unresolved binarism, 50% of the stars are assigned a companion star from the same IMF, with a mass ratio also randomly chosen in the range \( 0.6 \leq m_2/m_1 \leq 1.0 \). Extinction is drawn from the Schlegel et al. (1998) maps. In order to model populations of different ages and metallicities, the model used distinct SFHs and age–metallicity relations for each component (for details, see Girardi et al. 2005).

Figure 1 shows the on-sky distribution of model stars inside the DES footprint according to spectral type. The projection is shown in equatorial coordinates. Stripe 82 is the narrow region very close to the equator. The connection region is the square just to the south of it, extending to \( \delta = -20^\circ \). The main gradient in surface density seen in all panels follows Galactic latitude.

Figure 2 shows the TRILEGAL predictions for the differential number of stars, in logarithmic scale, as a function of \( r \) magnitude for the entire DES solid angle. We use a 0.1 mag bin width but express the numbers in unit mag bins. The total counts are shown as a solid line, whereas the contribution from each structural component is shown as indicated in the captions. The total number of model stars for each Galactic component is \( 3.13 \times 10^7 \) for the thin disk, \( 4.20 \times 10^7 \) for the thick disk, and

Figure 1. Spatial distribution of stars simulated within the DES area. The panels show stars of different spectral types: top left: O and B stars; top right: A and F stars; bottom left: G and K stars; bottom right: M and L stars.
4.65 × 10^7 for the halo. The figure shows that DES will probe stars in a magnitude range (r > 21) well dominated by thick disk and halo counts. Given that the stellar halo and even the thick disk have never been probed to such a large volume, the number of stars may increase if an unanticipated population of low-luminosity WDs or M dwarfs are found in these components. Such a population of cool halo dwarfs has in fact been suggested earlier, although it was later contested (Oppenheimer et al. 2001; Bergeron 2003).

The r − i color distribution is shown for the same model in Figure 3. The symbols and bin width are the same as in Figure 2. The numbers are also normalized to unit magnitude. At the blue end, r − i ≤ 0.6, the distribution is dominated by halo and thick disk stars close to the main-sequence turnoff (MSTO). The thin disk low-mass MS contributes with most of the stars in the range r − i ≥ 1.

4. STAR–GALAXY SEPARATION

The usefulness of DES to studies of the MW structure and resolved stellar populations in general depends strongly on the ability to explore its stellar sample to its full depth. This requires an efficient method to distinguish stars from galaxies and QSOs down to the faint DES detection levels. We here concentrate on star–galaxy separation, since galaxies are by far the main source of contamination to a stellar sample, especially at faint magnitudes (r > 22).

DES images are simulated as part of DES Data Challenges. These experiments serve as a means to test and improve on the survey’s data management pipelines. They also serve the purpose of evaluating the survey requirements (including object classification) and validating science analysis pipelines prior to the availability of real data. Data Challenge images attempt to be as realistic as possible, mimicking not only the expected geometry of DECam images, but also various instrumental effects including point-spread function variations due to atmospheric seeing and CCD position, combined transmission and response curves from filters, CCDs and telescope, and so on.

The input stellar sample to the Data Challenges was created with TRILEGAL. The input galaxy sample was generated by AddGals (M. Busha 2010, private communication), which is an algorithm for painting galaxies onto dark matter particles in an N-body simulation by matching galaxy luminosities with local dark matter densities, not dark matter halos. In addition to an N-body simulation, the algorithm takes as inputs a galaxy luminosity function, a luminosity-dependent correlation function, and a distribution of galaxy colors given luminosity and environment.

Tests with the latest set of such simulations, from Data Challenge 5 (DC5), have been carried out in order to assess how different star–galaxy classification parameters perform. The distributions of three different such parameters are shown separately for stars and galaxies in Figure 4. DES Data Management pipelines use SExtractor as their basic source detection and characterization tool. SExtractor outputs a stellarity index or class-star for each object it finds. This parameter is presented in Bertin & Arnouts (1996). Fluxradius is a measure of the half-light radius of each source. Finally, spread-model is a classifier adopted in SDSS (Scranton et al. 2002). A star–galaxy classification scheme depends not only on the adoption of a discriminating parameter but also on some cutoff value for this quantity. In the case of class-star, for instance, galaxies tend to have values close to zero, while the distribution of class-star values for stars concentrates close to unity. A typical cutoff value for selecting stars is class-star > 0.9.

To quantify the star–galaxy separation efficiency of a given parameter and cutoff value, we build completeness and purity curves. Completeness is defined as the ratio of the number of true stars classified as such in a given magnitude range to the total number of true stars in that range. Purity is defined as the ratio of the number of true stars classified as such in a given magnitude range to the total number of objects classified as stars in that range. The number of objects classified as stars is obtained by summing the number of objects classified as stars over all magnitude ranges. The number of true stars in a given magnitude range is obtained by summing the number of true stars over all magnitude ranges. The number of false stars in a given magnitude range is obtained by summing the number of false stars over all magnitude ranges.

Rossetto et al.

Figure 4. Distribution of different image-based classification parameters for stars and galaxies resulting from DC5 simulations. The distributions for stars (galaxies) are shown in dashed (dotted) lines. (a) Distribution of class-star; (b) spread-model; (c) fluxradius.

Completeness and purity curves from DC5 data are shown in Figure 5 as open and filled circles, respectively. The different panels correspond to different magnitude ranges, as indicated. The solid lines show the results of using class-star as a star–galaxy separator, the dashed lines show the curves based on fluxradius and the dotted ones are based on spread-model. The cutoff index along the x-axis depends on the parameter and its cutoff value used. For class-star, whose domain is in the range [0, 1], we define the cutoff index as \((\text{class-star} - 0.40)/0.03\). Therefore, an index value of zero means an extreme situation where a selection of class-star > 0.4 was used for the stellar sample. In the case of fluxradius, the mapping into cutoff index is given by \((3 - \text{fluxradius})/0.1\). And for spread-model, we use \((0.4 - \text{spread-model})/0.02\). These transformations always map the parameters onto the [0, 20] range in cutoff index, thus allowing the completeness and purity curves to be plotted together.

We notice from Figure 5 that completeness and purity compete with one another. A loose cutoff index (close to zero) makes the stellar sample complete, but very contaminated. A stringent cutoff, on the other hand, has the opposite effect. The point where these two curves cross indicates a good compromise between the two quantities. The DC5 results shown in the figure indicate that spread-model and fluxradius better discriminate among extended and point sources at bright magnitudes (first three panels), whereas class-star performs better at faint magnitude levels. For \(r < 22\), a simultaneous value of 80% in completeness and purity is easily achieved. At the faintest magnitude bin, however, this value drops to 65%.

An improvement to the object classification scheme stems from using color information to pre-select a star enriched sample. Color–color diagrams of stars and galaxies from the DC5 simulations show that the stellar locus is better defined in the \((i - z)\) versus \((r - i)\) panel. We then pre-select a star enriched subset of the data using this diagram.

Figure 6 shows completeness and purity curves for the same three object classifiers as in Figure 5 but now applied to the color pre-selected sample. Since a large chunk of the galaxy sample was eliminated from the sample based on colors, the purity values are boosted relative to the previous figure. The overall behavior of the curves remains but now an 80% pure and complete stellar sample is obtained down to \(r = 23\). Class-star still does a better job in separating stars from galaxies at low S/N levels, leading to a complete and pure stellar sample at the 72% level.

The star–galaxy separation experiments we carried out so far do not yet take into account all the color information that may be used to classify the sources. Another alternative, which we are currently exploring, is to abandon the classification paradigm and use these image parameters, along with colors, magnitude, and positions to assign probabilities of objects being stars, galaxies, and QSOs. In what follows, however, we will conservatively assume that the stars in our Galactic model will suffer from a 30% incompleteness and an equal amount of contamination by extragalactic sources.

5. THE STELLAR AND SUB-STESSIONAR LUMINOSITY FUNCTIONS

Given that stars can be successfully separated from galaxies and QSOs down to the nominal survey photometric depth, DES
Figure 5. Completeness and purity curves are shown in open and filled circles, respectively, for different classification parameters and for different magnitude ranges. The magnitude ranges are indicated in each panel. The curve types are the same in all panels: solid: class-star; dashed: fluxradius; dotted: spread-model. In the faintest magnitude bin ($23 < r < 24$; lower right panel), notice how class-star (solid lines) leads to a simultaneous purity and completeness of 63%, performing better than spread-model (60%) and fluxradius (51%).

Figure 6. Same curves and conventions as in Figure 5 but now using a color-based pre-selection meant to boost the fraction of stars. Completeness and purity curves are shown as open and filled circles, respectively, for different classification parameters and for different magnitude ranges. The magnitude ranges are indicated in each panel. The curve types are the same in all panels: solid: class-star; dashed: fluxradius; dotted: spread-model.
will provide stellar samples several times deeper than SDSS. The deep DES images will sample a large number of MS M stars, whose mass is slightly above or at the hydrogen burning limit, imposing stronger constraints than previous data on the very faint end of the thick disk and halo stellar luminosity functions. DES will also significantly increase the census of sub-stellar objects such as L and T dwarfs and WDs close to or at the end of the cooling sequence. Table 2 below lists these interesting stellar types whose luminosity function is still relatively unconstrained by current surveys. Table 2 below lists these interesting stellar types whose luminosity function is still relatively unconstrained at the faint end (\(M_V > 15\)), especially in the thick disk and halo components. The DES depth limits were calculated by taking into account the survey limits in each filter and the minimum requirement that at least one color index is needed to select candidates. The values listed do not take extinction into account.

### 5.1. Cool Low-mass Stars

DES depth limits for M, L, or T dwarfs are based on the \(\min(i, z)\) detection limits. The absolute magnitudes were taken from Hawley et al. (2002). The depth values computed in this way may actually be an underestimate, since an alternative approach to pre-select such extremely cool objects is to find objects detected in \(z\) (or \(i\) and \(z\)) but which drop out at bluer wavelengths. Overall, the estimated DES depths are from three to eight times larger than those from SDSS as estimated by Hawley et al. (2002).

The larger depths available to DES will allow strong constraints on the slope of the thick disk and stellar halo IMF close to the hydrogen burning mass limit. In Figure 7, we show the expected number counts in the entire DES footprint based on two slightly different assumptions for the IMF slope of the thick disk and halo populations in the mass interval \(0.08 < m/m_\odot < 0.50\). We use the Kroupa (2001) IMF as a starting point, whose power-law slope in this mass range is \(d \log \phi(m)/d \log m = 1.3\). The dotted line shows the results based on the fiducial model (Section 3) but with the slope \(d \log \phi(m)/d \log m = 1.4\). The dashed line shows the results for \(d \log \phi(m)/d \log m = 1.2\). The difference in star counts caused by these subtle variations in the fiducial IMF slope is larger at the faint end of the magnitude distribution and at the \(1.0 \leq r - i \leq 1.6\) color range. This color range is typical of low-metallicity M dwarfs. In absolute terms, the number counts in the quoted mass range above are of \(\approx 7.5 \times 10^7\) stars in the entire DES footprint, using the reference IMF slope, and including thin disk stars. This is more than 50% of all DES stars. The difference in star counts shown in Figure 7 is \(\approx 3 \times 10^6\), which is only about 4% of the total counts of M and K dwarfs in the fiducial model. Still, this difference is three orders of magnitude larger than the associated Poisson fluctuations in the total number count.

This very large statistical significance resulting from subtle variations in the model IMF slope is not strongly affected if we incorporate the star/galaxy separation efficiency discussed in Section 4. If we conservatively assume a 50% photometric incompleteness for K and M dwarfs in the stellar halo on top of a 30% incompleteness caused by star/galaxy separation, the difference in star counts will drop by a factor of three, to \(\approx 10^6\) stars. In addition, if we now contaminate the K and M stellar sample by 30% of galaxies, the total number

### Table 2

<table>
<thead>
<tr>
<th>Type</th>
<th>Absolute Magnitude</th>
<th>Maximum Distance</th>
</tr>
</thead>
<tbody>
<tr>
<td>M0 dwarf</td>
<td>(M_r = 8.4; M_i = 8.0)</td>
<td>13.3 kpc</td>
</tr>
<tr>
<td>M9 dwarf</td>
<td>(M_r = 15.5; M_i = 14.0)</td>
<td>500 pc</td>
</tr>
<tr>
<td>L5 BD</td>
<td>(M_r = 18.0; M_i = 15.8)</td>
<td>160 pc</td>
</tr>
<tr>
<td>T0 BD</td>
<td>(M_r = 20.0; M_i = 17.5)</td>
<td>65 pc</td>
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<tr>
<td>T5 BD</td>
<td>(M_r = 23.0; M_i = 19.0)</td>
<td>16 pc</td>
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<tr>
<td>Pre-LF peak WD</td>
<td>(M_r = 13.0; M_i = 13.0)</td>
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<tr>
<td>Post-LF peak WD</td>
<td>(M_r = 16.5; M_i = 15.1)</td>
<td>180 pc</td>
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</table>
of $0.08 < m/m_\odot < 0.50$ stars in the fiducial model increases to $\simeq 10^3$. This means that the expected variation in star counts caused by the IMF change is still $\simeq 10^9/10^4 = 10^5$ times larger than the Poisson fluctuations the total model counts. We thus conclude that the observed DES star counts, especially in the color range quoted above, can be safely used to constrain the halo and thick disk IMF slope at low masses, with high statistical significance, to within a few hundredths of dex.

We carried out a similar exercise, but now varying the IMF slope in the sub-stellar regime, $0.01 < m/m_\odot < 0.08$. Our fiducial IMF predicts a power-law slope of 0.3 dex in this range for all Galactic components. This leads to $\simeq 3 \times 10^4$ BDs in our fiducial model, almost all of them belonging to the thin disk. An IMF variation of 0.2 dex leads to a 10% change in the number counts. Incorporating a factor of three decrease due to incompleteness leads to a difference of $\simeq 10^3$ in the number counts of these very red objects when the IMF is varied. This is a difference three orders of magnitude smaller in star counts than in the previous experiment. The expected Poisson fluctuations in the fiducial model will be of the order of $\sqrt{1.3 \times 3 \times 10^4} \simeq 100$, where the 1.3 factor again accounts for Galaxy contamination. Notice that this contamination will probably be smaller at the very red colors typical of L and T dwarfs (see below). Still these overestimated fluctuations are one order of magnitude smaller than the expected variation in the numbers of these objects. We may thus conclude that the census of very red faint objects in DES may be used to constrain the IMF slope of sub-stellar objects to the precision of about 0.1 dex.

It is useful to compare the color range of M, L, and T dwarfs to the expected colors of galaxies, since these latter will dominate the DES source counts at faint magnitudes. Newberg et al. (2002) analyzed about five million stars from SDSS close to the celestial Equator. The observed color–magnitude diagrams (CMDs) show that galaxies strongly dominate the source counts at relatively blue color ranges $0.4 < g - r < 1.0$, being much less numerous in the $g - r > 1.1$ range occupied by low-mass MS stars or by sub-stellar objects. We are currently in the process of quantifying the purity of the expected DES stellar sample when it is selected by a combination of stellar parameters from the images and observed colors. Our goal is to build a probability distribution function of a given DES source to be a star as a function of position, magnitude, and color.

5.2. White Dwarfs

For WD, the DES depths shown in Table 2 were computed using the min($g$, $i$) detection distance. Absolute magnitudes are from Bergeron et al. (1995) models for a purely hydrogen WD with $log g = 8$. We here assess the usefulness of DES filters to separate a sample of WDs from the other stellar types. WDs have much larger surface gravities and tend to be relatively blue compared to the bulk of the MS stars. In Figure 8, we compare the properties of WDs with those of normal stars in our fiducial Galactic model, described in Section 3. We do that both in the theoretical and in the observational space. Panel (a) shows the distribution of effective temperatures ($T_{\text{eff}}$) of MS stars and WDs, separated according to $log g$. This quantity clearly separates MS stars ($log g < 6$) from the WD cooling sequence ($log g > 6.5$ and $log L/L_\odot < 0$). The total number of WDs in our model is $7.6 \times 10^5$. The distributions as a function of $(g-r)$ colors are shown in panel (b). Notice that WDs outnumber MS stars by over an order of magnitude for $T_{\text{eff}} > 10,000$ K. However, the distributions are not so clearly segregated in color. Still, a cut in $(g-r) < 0$ will tend to select a sample of WDs with 20% contamination or less. The results from our simulations are in qualitative agreement with previous work based on SDSS colors by Harris et al. (2003), where it is shown that WDs hotter than $\simeq 12,000$ K segregate in color space from normal MS stars, blue horizontal branch (BHB), and QSOs. However, availability of the $u$ band is particularly useful to derive a cleaner sample of WDs and to separate them from BHBs and QSOs. Follow-up imaging with the DECam or availability of SkyMapper data will provide $u$-band magnitudes.

6. PROPER MOTIONS

Cool WDs are mixed with and largely outnumbered by halo stars close to the MSTO. As these WDs probe the faint end of the white dwarf luminosity function, they are extremely important as a tool for dating the thin and thick disks at different scale heights. The best means to disentangle such a cool WD population is to use PMs, since disk WDs, being at much shorter distances, will display larger PMs than the distant F and G halo stars (Kilic et al. 2006). Assuming a typical transverse velocity of $V_T = 20$ km s$^{-1}$ relative to the local standard of rest and a distance of $d = 100$ pc, leads to $\mu \simeq 40$ mas yr$^{-1}$. At larger distances perpendicular to the disk plane, similar values may be expected since the velocity dispersion also tends to increase. A cool halo WD at $d = 500$ pc with $V_T = 200$ km s$^{-1}$ will have...
Figure 9. Comparison of the TRILEGAL proper motion distributions (solid line) with the observed ones (dashed line). The upper panels show $\mu_\alpha \cos \delta$ distributions, whereas the lower panels show those in $\mu_\delta$. In the left (right) panels, the model is compared to UCAC3 (SDSS) data. The model was cut at $V = 17$ for the UCAC3 comparison and at $g = 22$ for SDSS in an attempt to simulate the typical depth of these reference data.

$\mu \simeq 80$ mas yr$^{-1}$. Such PMs are likely to be measurable over the five-year baseline of DES.

PMs will also be useful for separating BDs from high-redshift QSOs and very red galaxies. The expected PM values of BDs, which will be detected well within the thin disk (see Table 2) are similar to those of cool disk WDs, since they share similar kinematics and distances.

Given their importance to the selection of interesting stellar types, we have implemented and validated a kinematical model in the TRILEGAL code. Space velocities are randomly taken from the Schwarzschild velocity distribution appropriate for the age, position, and Galactic component of each simulated star. The velocity ellipsoids are taken from the literature, and assumed to be cylindrically symmetric with respect to the Galactic disk rotation axis.\footnote{This is probably a good approximation for the disk populations that will be observed by DES, but can certainly be improved for the stellar halo.} For the thin disk, the UVW velocities are taken from Holmberg et al. (2009), with an extrapolation for the oldest ages and truncated for the youngest, and suitably converted into the cylindrical $V_r$, $V_\phi$, $V_z$. The local $V_\phi$ is then increased/reduced as a function of the galactocentric radius, according to the galactic rotation curve from Dias & Lépine (2005). For the thick disk and halo, the velocity ellipsoids are taken from Chiba & Beers (2000).

Space velocities generated this way are then corrected by the motion with respect to the local standard of rest (from Dehnen & Binney 1998), and decomposed into radial and transverse components (see Johnson & Soderblom 1987). The latter is finally converted into PMs using the simulated stellar distance.

In Figure 9, we compare the model PMs with data. The panels on the left show the results for PMs from the third version of the U.S. Naval Observatory CCD Astrometric Catalog (UCAC3; Zacharias et al. 2010). The field is a 1 deg$^2$ region centered on $(l, b) = (352.5, -62.8)$, which is inside the region of the DC5 simulations, described in Section 4. The TRILEGAL data were cut at bright ($V < 17$) magnitudes in order to match UCAC3 depth. The model and observed PM distributions are very similar. The narrower peak in the model can be accounted for by the measurement errors which are not yet simulated. Notice that the spread in PMs is larger parallel to the Equator than it is perpendicular to it. The panels on the right of Figure 9 show the model comparison to SDSS PMs in a mirror field to the first one relative to the disk plane, $(l, b) = (352.5, +62.8)$. In this case, the model stars were cut at $g < 22$, again as an...
attempt to approximately mimic the SDSS sample. The model
and data PM distributions, both parallel and perpendicular to the
Equator, are again nearly identical apart from the lack of model
errors. The TRILEGAL kinematical mode was also validated in
other directions, including close to the Galactic and Equatorial
Poles, the Solar Apex, and directions close to the Galactic
center and anti-center. In all these directions, the model PMs
reproduced UCAC3 distributions very well. We also investigated
the dependence of the PM values with magnitude for a field in
the DES DC5 region and found that the PM distributions change
very little as a function of magnitude.

We are thus in a position to simulate the expected distributions
of PMs within the entire DES footprint and for different
stellar types, including WDs and BDs. These predictions will
then be compared with the observed ones resulting from DES
astrometry. It is likely that the best PM estimated for faint stars
such as WDs and BDs will result from DES itself. The reason
is the lack of earlier data sets with comparable depth in the
Southern Hemisphere. The current astrometric precision aimed
by DES data management is of \(\lesssim 50\) mas for the five-year stacks.
The survey strategy is still not entirely defined, so it is currently
not possible to couple the astrometric precision with a time
baseline and in order to assess the expected PM errors.

7. DISK AND HALO STRUCTURE

Models of the structure of the Galaxy require a large area
coverage in order to quantify the various parameters governing
the density profile and geometry of the different structural
components. The basic input for the tomography of the MW are
the star counts as a function of magnitude, colors, and direction
on the sky. Strong constraints on the model parameters can
be established using photometric parallaxes of stellar tracers
of each Galactic component. A recent and extensive work on
this line is that of Jurić et al. (2008). The authors derived scale
lengths, scale heights, and relative normalization for the thin and
thick disk components using the distribution of low-mass MS
stars (M dwarfs) sampled by SDSS out to \(\pm 2\) kpc. The structure
of the stellar halo, on the other hand, was constrained using F
and G stars close to the MSTO.

In an alternative approach, de Jong et al. (2010) applied a
CMD fitting technique to the SEGUE (Yanny et al. 2009) sample
in order to constrain the structure of the thick disk and stellar
halo. This technique models the Galactic components at once by
building artificial CMDs at different directions and statistically
comparing them to the observed ones.

One point of discrepancy among different authors is the shape
of the stellar halo. de Jong et al. (2010) favor an oblate halo with
an axis ratio of \(c/a = 0.88\) within the inner 25 kpc. Jurić et al.
(2008) best-fitting models are also oblate but flatter; \(c/a = 0.64\).
Finally, Du et al. (2008) find a varying stellar halo shape with
evidence of a lower \(c/a \approx 0.4\) toward the center of the Galaxy
and \(c/a \approx 0.6\) in the opposite direction.

Figure 10 shows predicted star counts for DES with two
different assumptions for an oblate halo axial ratio: \(c/a = 0.65\)
(which is our reference value) and \(c/a = 0.70\). The difference
between the two models becomes clearer for \(r > 21.0\), where
halo counts start to become significative compared to the other
components, but, again, the best bet for constraining the halo
structure is to use color counts, in this case in the range
\(0 < r - i < 0.6\), which is dominated by F and G stars close
to the halo MSTO. About \(4 \times 10^7\) stars are found in this color
range, while the difference in number counts between the two
models is at the 10% level. As in the case of the M dwarfs,

\[
\begin{align*}
\text{log } N(r) \text{ (mag}^{-1}) &= 8 \\
\text{log } N(r-i) \text{ (mag}^{-1}) &= 8
\end{align*}
\]

Figure 10. Upper panel: model star counts as a function of \(r\) magnitude in the
entire DES solid angle for two different choices of an oblate halo axis ratio, \(c/a\).
Dotted line: \(c/a = 0.7\); dashed line: \(c/a = 0.65\). The bin size is 0.1 mag. The
inset at the bottom right is a blow up in the range \(r > 22\), where the differences
are more pronounced. Lower panel: star counts as a function of \(r - i\) color for
the same models as in the previous panel. The inset at the bottom right is a blow
up in the color range where the differences are more pronounced.

...
to be compared with the \(\sim \sqrt{1.3 \times 4 \times 10^7} \approx 7 \times 10^3\) Poisson fluctuation in these number counts.

DES will allow comparison of star counts between the Southern and Northern hemispheres to a precision and volume not previously obtainable. Xu et al. (2007) noted evidence for a significant asymmetry in halo star counts between north (using SDSS) and south. Unfortunately, the work relied on the use of photographic plate data in the south, and it was difficult to compare to the deeper, more precise CCD data in the north. DES will offer a vastly improved CCD data set in the griz filters in the south, which we will explore in detail, and compare against models. Similarly, some recent studies also discuss a possible triaxiality in the thick disk (Parker et al. 2003, 2004; Larsen et al. 2010), which again will be better investigated with a combined sample covering both hemispheres.

Any global asymmetry found in the structure of the stellar halo can be used as input into Galactic formation models, and opens the door to quantitatively explore triaxial dark matter halos, as well as a possible misalignment between a dark matter halo and the MW stellar disk.

7.1. Halo Substructure

Several substructures are expected to exist and have been found in the more extended Galactic components, especially in the halo. In particular, the currently most successful scenario for structure formation in the universe, the \(\Lambda\)CDM model, predicts that large galaxies form by the agglutination of sub-galactic fragments, specially during their early evolutionary history. Consistently with this picture, numerous new and unexpected streams of stars have been detected in the Northern Galactic Cap using the SDSS data.

The Sagittarius tidal stream is the most prominent structure, running from \((l, b) = (200^\circ, 30^\circ)\) to \((l, b) = (340^\circ, 60^\circ)\). The Sagittarius tidal stream is also prominent in the south, and crosses through the DES survey area. Also visible are the Orphan Stream, running perpendicularly from \((l, b) = (255^\circ, 48^\circ)\) to \((l, b) = (195^\circ, 48^\circ)\), and the Virgo overdensity at \((l, b) = (300^\circ, 60^\circ)\), among others.

DES will be able to carry out a similar survey and detect streams in the south to even fainter depths. The fundamental physics obtainable from modeling the orbits of these streams are constraints on the shape of the dark matter halo in which the tracer stream stars move. Work on streams in the north indicates that several streams at different inclinations are needed to probe the potential accurately.

New satellites of the Galaxy will also be discovered with the stellar DES sample. SDSS has yielded a total of 14 new dwarf spheroidals or transition objects between low-mass galaxies and globular clusters (see Walsh et al. 2009, and references therein). An analysis by Tollerud et al. (2008) results in an estimate between 19 and 37 new satellites to be discovered in DES assuming that the characteristics of detectability are the same as in SDSS. On the other hand, the deeper DES sampling should increase the contrast of these objects relative to halo field stars, since DES will probe further down the stellar luminosity function. In particular, DES will be able to probe the stellar MS of an old population at distances out to \(\approx 120\) kpc. This will lead to a much faster increase in the number of satellite stars as compared to the contaminating background. Assuming a power-law IMF, \(\Delta N/\Delta m \propto m^{-\alpha}\) and a simple power-law MS mass–luminosity relation \(L \propto m^\beta\), we can integrate the IMF in order to estimate the number of sampled stars in a given population. The lower limit of the integral is the lowest MS mass which leads to detection (given the satellite distance and the sample magnitude limit). The upper limit will be the highest MS mass which has not yet turned into a degenerate (which decreases with age) The relative increase in the number counts of stars for two surveys with magnitude limits \(m_1\) and \(m_2 > m_1\) is then

\[
\frac{\Delta N_{\text{SDSS}}}{N_o} = \frac{10^{-0.4 \frac{\Delta m_{m_2}}{\beta}} - 10^{-0.4 \frac{\Delta m_{m_1}}{\beta}}}{10^{-0.4 \frac{\Delta m_{m_1}}{\beta}} - 10^{-0.4 \frac{\Delta m_{m_2}}{\beta}}},
\]

where \(m_{\text{bd}}\) in the denominator is the MS magnitude of the brightest star in the population. If we assume that this second term on the denominator is zero \((m_1 > m_{\text{bd}}\)), which is the same as saying that the number of degenerates is insignificant) and use \(\alpha = 2.35\) (Salpeter IMF), \(\beta = 3.5\), \(m_1 = 22.5\) (SDSS), and \(m_2 = 24\) (DES), one obtains \(\Delta N_{\text{SDSS}}/N_o = 0.7\). In other words, considering that the background counts of stars vary much more slowly, DES will increase the density contrast of MW satellites by a factor of 1.7 relative to SDSS out to a distance modulus of \((m - M)_0 \approx 20\). This factor will be larger if we relax the assumption that the satellite has no degenerates. We thus conclude that DES will be particularly more efficient than SDSS in detecting very low mass satellites at distances about twice as large as those to the Magellanic Clouds.

Detection of satellites situated further away will not be as significantly improved unless they have young or intermediate age stellar populations, for which the previous argument would apply to a more luminous MS locus. One interesting possibility that also needs to be further investigated is any dependence of typical satellite size with distance from the MW. A trend of smaller clusters having more concentrated spatial distributions has been observed in extragalactic cluster systems and may as well apply to MW satellite galaxies and transition objects (Larsen & Brodie 2003; Jordán et al. 2005). This would make the more distant MW satellites of lower surface brightness at a fixed mass than their more nearby counterparts, something that would jeopardize their detection. We are currently in the process of investigating the detection of MW satellites with DES in more detail, by taking selection effects with surface brightness and SFH into account.

8. SUMMARY AND CONCLUSIONS

In this paper, we have utilized a theoretical model to forecast the main contributions that DES will give to studies of Galactic structure and resolved stellar populations. We adopted a fiducial Galactic model based on the TRILEGAL code, as described in Section 3. It predicts \(\approx 1.2 \times 10^5\) total stars within the DES footprint. Thin disk star counts will be dominated by low-mass MS stars with \(m \lesssim 0.5\ M_\odot\), but such low-mass stars will also be sampled in large numbers in the thick disk and halo, and beyond about 10 kpc. Consequently, we have shown that the IMF slope at low masses will be constrained to within a few hundredths of dex in the thick disk and halo.

About \(3 \times 10^5\) L and T dwarfs will also be sampled by DES, the vast majority of them belonging to the thin disk. This will again allow a strong constraint to the IMF in the sub-stellar regime. We estimate that the sampling depth of low-mass and low-luminosity species, such as M, L, and T dwarfs or WDs, will be from three to eight times larger than those quoted for SDSS in the literature. The Galactic model we adopted was also used to discuss the capacity of detection of WDs using griz\(Y\) colors. We conclude that a sample of hot WDs, with a contamination of about 20% or less, can be selected without the \(u\) band. We also present the initial results of our model PMs and compare
them to observed ones from UCAC3 and SDSS toward several directions in the Galaxy. In all cases, the model PMs agree with the data. We argue in favor of using the PMs determined from DES as a means to detect cool WDs and to separate BDs from high-redshift QSOs.

We have also addressed one of the main issues for stellar studies in a deep photometric survey such as DES: star–galaxy separation. We used the latest set of DES image and catalog simulations to quantify completeness and purity of a stellar sample as selected with different image classification parameters. We conclude that a global stellar sample which is simultaneously pure and complete at the 70% will easily be achieved. We also discussed the effect of the remaining contamination on the science results. More specific stellar samples may be further refined on the basis of the multi-dimensional color space available from DES. One example is the use of color information in association with image-based stellarity parameters, which will likely allow red stellar and sub-stellar objects to be more efficiently separated from most galaxies.

Thick disk and halo stars will be dominated by F and G stars close to the MSTO point. One of the main contributions from these objects will be to probe the halo structure and substructure to very large distances. Our models show that DES star counts will constrain the halo shape to very high accuracy. For instance, an oblate halo will have its axial ratio determined to within 1%–2%, assuming an efficient star/galaxy separation down $r \simeq 23.5$. Asymmetries in star counts as a function of direction on the sky and magnitude, including those based on a joint DES/SDSS sample, will constrain halo triaxiality as well as thick disk azimuthal variations.

Finally, we discuss the impact that DES will have on the detection of new halo substructure, including new star clusters and low-mass galaxies. We conclude that DES will increase the density contrast of these objects by about 60% or 70% when compared to SDSS for distances lower than $\simeq 120$ kpc. This is the result of DES reaching the stellar MS of an old stellar population within this distance range. This enhanced efficiency distance limit may increase for satellites that harbor young or intermediate age stellar populations.

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